Common types of recurrences

Algorithms and Complexity Theory

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  - Try to *get rid* of unwanted terms